



# FORMAL METHODS INTRODUCTION

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PROFESSOR

(MANY YEARS COLLABORATION IN PARTICULAR WITH JOHN FITZGERALD)



# WHO AM I?

- › **Professor Peter Gorm Larsen; MSc, PhD**
- › 20+ years of professional experience
- › ½ year with Technical University of Denmark
- › 13 years with IFAD
- › 3,5 years with Systematic
- › 7 years with Aarhus School of Engineering
- › Reviewer for EU on Research projects and applications
- › Consultant for most large defence contractors on large complex projects (e.g. US Joint Strike Fighter)
- › Relations to industry and academia all over the world
- › Has written books and articles about VDM
- › See <http://pglconsult.dk/private/peter.htm> for details



# FORMAL METHODS INTRODUCTION

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## ➤ **Formal Methods Characteristics**

- › Formal Methods Europe
- › Tool Support for FM

# WHAT ARE FORMAL METHODS?

- › **Formal Methods** refers to the use of techniques from logic and discrete mathematics in the specification, design and development of computer systems and software.
- › Mathematics is NOT as difficult as many thinks
- › Mastering of **complexity** using **abstraction**.
- › Reduce argumentation to a **calculation** which can be checked by mechanical means.
- › Replace manual reviews with a **repeatable** analysis.
- › Formal methods can be used at different levels of **rigour**.

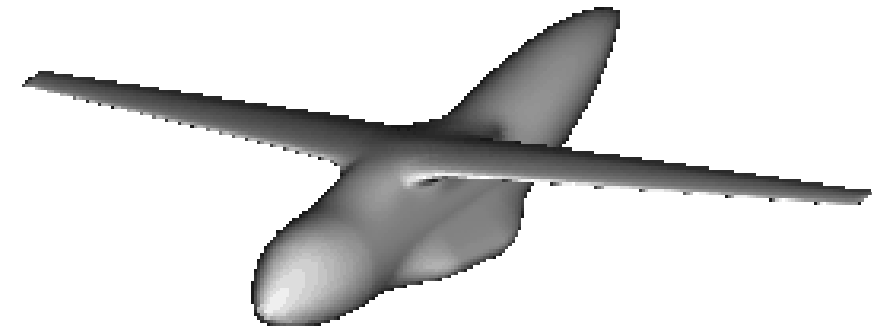
# VALIDATION TECHNIQUES

- › **Inspection:** organized process of examining the model alongside domain experts.
- › **Static Analysis:** automatic checks of syntax & type correctness, detect unusual features.
- › **Testing:** run the model and check outcomes against expectations.
- › **Model Checking:** search the state space to find states that violate the properties we are checking.
- › **Proof:** use a logic to reason symbolically about whole classes of states at once.

# LEVELS OF RIGOUR

- > **Level 1:** Use of concepts and notation from discrete maths
- > **Level 2:** Use of formalized abstract specification languages with some mechanized support tools
- > **Level 3:** Verification of the abstract precise specification
- > **Level 4:** Fully formal development (refinement from abstract specifications)

# MODELLING COMPUTING SYSTEMS



# MODELLING COMPUTING SYSTEMS

- › In other engineering disciplines (Mechanical, Electrical, Aeronautical etc.) system **models** are built *to help gain confidence* in requirements and designs.
- › For example: wind tunnels, stress models
- › Two characteristics of these models are crucial to their successful use: **abstraction** and **rigour**.



# ABSTRACTION

Engineering models omit details that are not relevant to the **purpose** of the model.

For example:

- › Windtunnel – assess aerodynamics
- › Cockpit mockup – assess human factors, train pilots

The omission of detail not relevant to a model's purpose is called **abstraction**. The choice of which details to omit is a matter of *engineering skill*.

See for example: “Abstraction – the key to Computing?”, by Jeff Kramer

# ABSTRACTION

Compare these extracts from two descriptions of the same system.

*The FlightFinder System is to be used by travel agents and their customers. Details are entered, including point of departure, destination, preferred dates and times. The system will respond with a range of itineraries and fares, along with the relevant restrictions.*

“What”

The system records locations as nodes in a connected graph structure. Each node struct contains an array of pointers to reachable destinations plus, for each pointer, a timetable of flights stored as a hash table. Each record in the hash table has a flight number (8 character string), departure and arrival times (standard time formats) and operating dates (standard date format). To obtain the optimal route, the graph must be traversed using a shortest path algorithm on a modified adjacency matrix ...

“How”

# RIGOUR

The most important property of a model of a computing system is its **suitability for analysis**: must be

- › objective (not down to the opinion of individual engineers)
- › repeatable
- › susceptible to machine support.

The language in which a model is described should be **rigorously defined**:

- › little room for disagreement about what a model actually says
- › analysis tools reach the same conclusion about model's properties



# MATHEMATICAL REPRESENTATION OF SOFTWARE

- › Formal specifications are expressed in a mathematical notation with precisely defined vocabulary, syntax and semantics.
- › **Algebraic** approach
- › The system is specified in terms of its operations and their relationships.
- › **Model-based** approach
- › The system is specified in terms of a state model that is constructed using mathematical constructs such as sets and sequences.

# CLASSES OF FORMAL METHODS

- › Model-based approaches (VDM, Z, B)
- › Algebraic approaches (Act One, Larch, OBJ)
- › Process algebras (CSP, CCS)
- › Logic-based approaches (RTL, TLA)
- › Reactive approaches (Petri-nets, SDL, SAO)
  
- › Combinations like RAISE (VDM + CSP) and LOTOS (Act One + CCS).
- › ISO standards for VDM, Z, LOTOS and ITU standard for SDL
  
- › Different strengths
- › Very different kind of tool support

# FORMAL METHODS IN ACADEMIA

- › Tradition with Abstract Models in Europe
- › Focus on Formal Development
- › US focus on Automatic Verification
- › FM taught at many European Universities
- › Spreading from the UK
- › Japan usage and supply gaining strength
- › Different opinions about way ahead (e.g. Parnas, “Really rethinking formal methods”, IEEE Computer January 2010)

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✓ **Formal Methods Characteristics**

➤ **Formal Methods Europe**

> **Tool Support for FM**



# FORMAL METHODS EUROPE

- › [www.fmeurope.org](http://www.fmeurope.org)
- › FME = Formal Methods Europe
- › Stimulate the use of formal methods by industry.
- › Promote international co-operation among researchers and users of formal methods.
- › Exchange ideas & identify common interests.
- › Provide links between research and application areas.
- › Conference approximately every 18 months





# FME (VDM) CONFERENCES

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<b>Brussels, Belgium</b>	<b>(1987)</b>	<b>LNCS 252</b>
Dublin, Ireland	(1988)	LNCS 328
Kiel, Germany	(1990)	LNCS 428
Noordwijkerhout, Netherlands	(1991)	LNCS 551/2
Odense, Denmark	(1993)	LNCS 670
Barcelona, Spain	(1994)	LNCS 873
Oxford, UK	(1996)	LNCS 1051
Graz, Austria	(1997)	LNCS 1313
Toulouse, France	(1999)	LNCS 1708/9
Berlin, Germany	(2001)	LNCS 2021
Copenhagen, Denmark	(2002)	LNCS 2391
<b>Pisa, Italy</b>	<b>(2003)</b>	<b>LNCS 2805</b>
Newcastle, UK	(2005)	LNCS 3582
Hamilton, Canada	(2007)	LNCS 4085
Turku, Finland	(2008)	LNCS 5014
Eindhoven, Netherlands	(2009)	LNCS 2850
Limerick, Ireland	(2011)	LNCS 6664
Paris, France	(2012)	LNCS 7436
<b>Singapore</b>	<b>(2014)</b>	

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# FORMAL METHODS TOOL SUPPORT

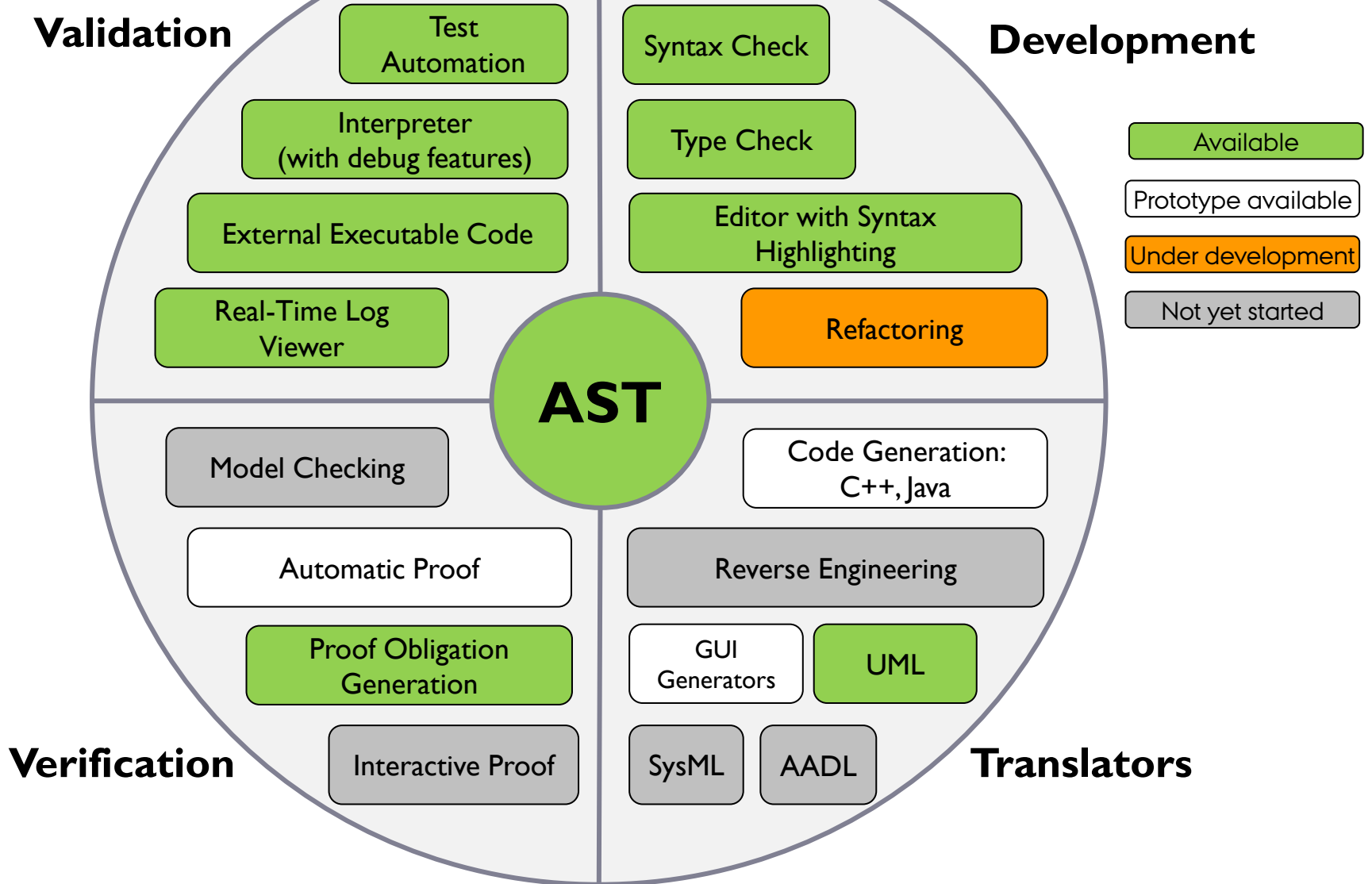
- › VDMTools from SCSK
- › Atelier-B from ClearSy
- › FDR from Formal Systems Europe
- › SCADE from Esterel Technologies
- › Lots of prototype/academic tools
- › Overture open-source development for VDM

# FORMAL METHODS TOOL FEATURES

- › Syntax checking
- › Type checking
- › Proof obligation generation
- › Proof support
- › Model checking
- › Pretty printing
- › Animation/Execution
- › Refinement
- › Test automation
- › Code generation
- › Graphical User Interface

## Validation

## Development



# TAKE AWAY POINTS

- › There is nothing magic about formal methods
- › It is just a sensible **engineering** approach
- › Strong European FM supplier side
- › USA still strongest on model checking for hardware
- › Japan usage and supply gaining strength
- › Tools are essential for success
- › Consider attending FM 2014 in Singapore

# THANKS FOR YOUR ATTENTION



## Any questions?